



Answer all the following questions

Q1. (25 marks) Given $x_1(n) = 1 + 2\cos(\pi n) + \cos\left(\frac{\pi}{2}n - \frac{\pi}{2}\right)$,

$$x_2(n) = [1 \ 0 \ 1]$$

$$x_3(n) = 2\delta(n) + 2u(n) - 2u(n-1)$$

- (i) Find one period of $x_1(n)$.
- (ii) Calculate the power of $x_1(n)$.
- (iii) Sketch $x_1(n) + x_2(n) + x_3(n)$.
- (iv) Find $x_1(n) * x_2(n)$.
- (v) Find $X_1(z) X_2(z)$.

Hint: the z-transform of $\delta(n) = 1$

Q2. (15 marks) One period of a periodic discrete signal:

$$x(n) = 1 \quad \text{for } n = 0, 2, 3$$

$$0 \quad \text{for } n = 1$$

- (i) Sketch the discrete signal $x(n)$.
- (ii) Use the DFT general formula or the 4-point radix-2 FFT to compute $X(k)$.
- (iii) Calculate the power in frequency domain.

Q3. (20 marks) The Pole-Zero plot of a digital filter $H(z)$ is shown in Fig.1.

- (i) Make a sketch of the magnitude of the frequency response $|H(\Omega)|$.
- (ii) Determine the linear difference equation.
- (iii) Draw the implementation structure (Block Diagram) of the Digital filter.

